

Functional Thinking

NEAL FORD software architect / meme wrangler

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tortured

3 ^ metaphors

assign to x

$$x := x + 1$$

solve for x?





Paradigms

~~Languages are
tools.~~

Learning a new
one takes time.

"functional" is
more a way of
thinking than
a tool set

Execution in the Kingdom of Nouns

Steve
Yegge

[http://steve-yegge.blogspot.com/
2006/03/execution-in-kingdom-of-nouns.html](http://steve-yegge.blogspot.com/2006/03/execution-in-kingdom-of-nouns.html)



verbs!

"OOP makes
working with
state easier.

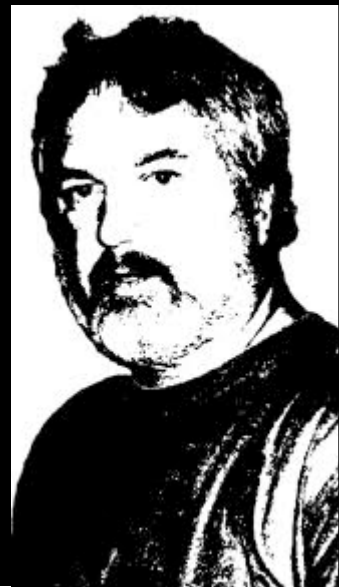
FP makes
eliminating state
easier"

OH on **twitter**

OO makes code
understandable by
encapsulating moving
parts.

FP makes code
understandable by
minimizing moving
parts.

Michael Feathers, author of "Working with Legacy Code"



4

1

3

8

number
classification

perfect #

$$\Sigma(f(\#)) - \# = \#$$

(sum of the factors of a #) - # = #

(sum of the factors of a #) = 2#

$$6: 1 + 2 + 3 + 6 = 12 \ (2 \times 6)$$

$$28: 1 + 2 + 4 + 7 + 14 + 28 = 56 \ (2 \times 28)$$

$$496: \dots$$

classification

$$\Sigma(f(\#)) = 2\# \quad \text{perfect}$$

$$\Sigma(f(\#)) > 2\# \quad \text{abundant}$$

$$\Sigma(f(\#)) < 2\# \quad \text{deficient}$$

imperative

```
public class Classifier6 {  
    private Set<Integer> _factors;  
    private int _number;
```

```
public Classifier6(int number) {  
    if (number < 1)  
        throw new InvalidNumberException(  
            "Can't classify negative numbers");  
    _number = number;  
    _factors = new HashSet<Integer>();  
    _factors.add(1);  
    _factors.add(_number);  
}
```

```
public boolean isPerfect() {...
```

```
public boolean isAbundant() {...
```

```
public boolean isDeficient() {...
```

```
public static boolean isPerfect(int number) {...
```

```
}
```

```
public class Classifier6 {  
    private Set<Integer> _factors;  
    private int _number;  
  
    public Classifier6(int number) {...
```

```
private boolean isFactor(int factor) {  
    return _number % factor == 0;  
}
```

```
public Set<Integer> getFactors() {  
    return _factors;  
}
```

```
public boolean isPerfect() {...
```

```
public boolean isAbundant() {...
```

```
public boolean isDeficient() {...
```

```
public static boolean isPerfect(int number) {...
```

```
}
```

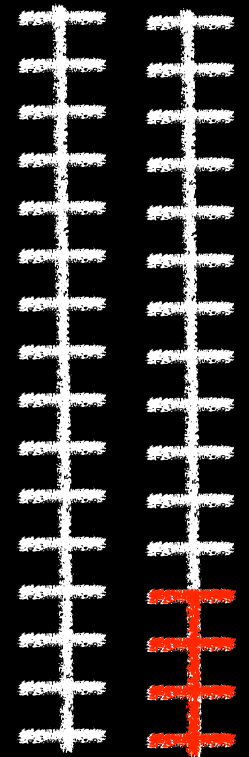
```
public class Classifier6 {  
    private Set<Integer> _factors;  
    private int _number;  
  
    public Classifier6(int number) {...  
  
    private boolean isFactor(int factor) {...  
  
    public Set<Integer> getFactors() {...
```

```
        private void calculateFactors() {  
            for (int i = 2; i < sqrt(_number) + 1; i++)  
                if (isFactor(i))  
                    addFactor(i);  
        }  
  
        private void addFactor(int factor) {  
            _factors.add(factor);  
            _factors.add(_number / factor);  
        }
```

```
    }
```

8

2




```
public class Classifier6 {  
    private Set<Integer> _factors;  
    private int _number;  
  
    public Classifier6(int number) {...  
  
    private boolean isFactor(int factor) {...  
  
    public Set<Integer> getFactors() {...  
  
    private void calculateFactors() {...  
  
    private void addFactor(int factor) {...
```

```
        private int sumOfFactors() {  
            calculateFactors();  
            int sum = 0;  
            for (int i : _factors)  
                sum += i;  
            return sum;  
        }  
    }
```

```

public class Classifier6 {
    private Set<Integer> _factors;
    private int _number;

    public Classifier6(int number) {...

    private boolean isFactor(int factor) {...

    public Set<Integer> getFactors() {...

    private void calculateFactors() {...

    private public boolean isPerfect() {
        return sumOfFactors() - _number == _number;
    private }

    public public boolean isAbundant() {
    public     return sumOfFactors() - _number > _number;
    public }
    public

    public public boolean isDeficient() {
    public     return sumOfFactors() - _number < _number;
    }
}

```

```
public class Classifier6 {  
    private Set<Integer> _factors;  
    private int _number;  
  
    public Classifier6(int number) {...  
  
    private boolean isFactor(int factor) {...  
  
    public Set<Integer> getFactors() {...  
  
    private void calculateFactors() {...  
  
    private void addFactor(int factor) {...  
  
    private int sumOfFactors() {...  
  
    public boolean isPerfect() {...  
  
    public boolean isAbundant() {...  
  
    public boolean isDeficient() {...  
  
    public static boolean isPerfect(int number) {...  
}
```



internal state

cohesive

composed

testable

refactorable

(slightly more)
functional

```
public class NumberClassifier {
```

```
    public boolean isFactor(int number, int potential_factor) {  
        return number % potential_factor == 0;  
    }
```

```
    public int sum(Set<Integer> factors) {...
```

```
    public boolean isPerfect(int number) {...
```

```
    public boolean isAbundant(int number) {...
```

```
    public boolean isDeficient(int number) {...
```

```
}
```



```
public class NumberClassifier {
```


```
    public boolean isFactor(int number, int potential_factor) {...
```

```
    public Set<Integer> factors(int number) {  
        HashSet<Integer> factors = new HashSet<Integer>();  
        for (int i = 1; i <= sqrt(number); i++)  
            if (isFactor(number, i)) {  
                factors.add(i);  
                factors.add(number / i);  
            }  
        return factors;  
    }  
}
```

```
public class NumberClassifier {  
    public boolean isFactor(int number, int potential_factor) {...  
    public Set<Integer> factors(int number) {...  
  
    public int sum(Set<Integer> factors) {  
        Iterator it = factors.iterator();  
        int sum = 0;  
        while (it.hasNext())  
            sum += (Integer) it.next();  
        return sum;  
    }  
}
```

```
public class NumberClassifier {  
    public boolean isFactor(int number, int potential_factor) {...  
    public Set<Integer> factors(int number) {...  
    public boolean isPerfect(int number) {  
        return sum(factors(number)) - number == number;  
    }  
    public boolean isAbundant(int number) {  
        return sum(factors(number)) - number > number;  
    }  
    public boolean isDeficient(int number) {  
        return sum(factors(number)) - number < number;  
    }  
}
```

no internal
state



```
public class NumberClassifier {  
    static public boolean isFactor(int number, int potential_factor) {...  
    static public Set<Integer> factors(int number) {...  
    static public int sum(Set<Integer> factors) {...  
    static public boolean isPerfect(int number) {...  
    static public boolean isAbundant(int number) {...  
    static public boolean isDeficient(int number) {...  
}
```

less need for scoping refactorable testable

"functional" is
more a way of
thinking than
a tool set

1st class
functions

pure
functions

concepts

strict evaluation

recursion

high-order
functions



$$K = \frac{1}{2} M v^2 + \frac{1}{2} I \omega^2$$

$$\frac{d^2 v}{d\varphi^2} = -\frac{1}{v^2} \left(\frac{v}{r} \right)^2 \frac{d^2 w}{d\varphi^2} \Rightarrow \frac{d^2 w}{d\varphi^2} + w = \frac{\mu G M m}{\gamma^2}$$

$$\vec{S} = \vec{N} \quad \text{and} \quad \frac{I_2 - I_1}{I_1} \omega_1$$

A diagram of a pendulum bob suspended by a string. The string is labeled $k \cdot \theta$ and $G \cdot \theta$. The angle between the string and the vertical is labeled θ . The bob is labeled M .

$$\frac{d^2 w}{d\varphi^2} = \frac{1}{v^2} \frac{d^2 b}{d\varphi^2} + \frac{2}{v^3} \left(\frac{db}{d\varphi} \right)^2$$

$$k = \frac{1}{2} M \dot{x}^2 = \frac{1}{2} M \left[\omega_0 A \cos(\omega_0 t + \varphi) \right]^2$$

$$\int_{-\infty}^{\infty} \delta(x) dx = 1 \quad (1)$$

n-order functions

high-order functions

functions that can
either take other
functions as
arguments or return
them as results

```
public void addOrderFrom(ShoppingCart cart, String userName,  
                        Order order) throws Exception {  
    setupDataInfrastructure();  
    try {  
        add(order, userKeyBasedOn(userName));  
        addLineItemsFrom(cart, order.getOrderKey());  
        completeTransaction();  
    } catch (Exception condition) {  
        rollbackTransaction();  
        throw condition;  
    } finally {  
        cleanUp();  
    }  
}
```




```
public void wrapInTransaction(Command c) throws Exception {
    setupDataInfrastructure();
    try {
        c.execute();
        completeTransaction();
    } catch (Exception condition) {
        rollbackTransaction();
        throw condition;
    } finally {
        cleanUp();
    }
}
```

```
public void addOrderFrom(final ShoppingCart cart,
    final String userName, final Order order) {
    wrapInTransaction(new Command() {
        public void execute() {
            add(order, userKeyBasedOn(userName));
            addLineItemsFrom(cart, order.getOrderKey());
        }
    });
}
```



```
def wrapInTransaction(command) {  
    setupDataInfrastructure()  
    try {  
        command()  
        completeTransaction()  
    } catch (Exception ex) {  
        rollbackTransaction()  
        throw ex  
    } finally {  
        cleanUp()  
    }  
}
```

```
def addOrderFrom(cart, userName, order) {  
    wrapInTransaction {  
        add order, userKeyBasedOn(userName)  
        addLineItemsFrom cart, order.getOrderKey()  
    }  
}
```

UndoManager.execute()

undo()




```
def addOrderFrom(cart, userName, order) {  
  wrapInTransaction {  
    add order, userKeyBasedOn(userName)  
    addLineItemsFrom cart, order.getOrderKey()  
  }  
}
```

What's so special about...

closures

```
def makeCounter() {  
    def very_local_variable = 0  
    return { very_local_variable += 1 }  
}
```

```
c1 = makeCounter()  
c1()  
c1()  
c1()  
  
c2 = makeCounter()
```

```
println "C1 = ${c1()}, C2 = ${c2()}"
```

```
closures » groovy MakeCounter.groovy  
C1 = 4, C2 = 1
```



```
public class Counter {  
    public int varField;  
  
    public Counter(int var) {  
        varField = var;  
    }  
  
    public static Counter makeCounter() {  
        return new Counter(0);  
    }  
  
    public int execute() {  
        return ++varField;  
    }  
}
```



Let the
Language
manage state

Languages handle

memory allocation

garbage collection

concurrency

state

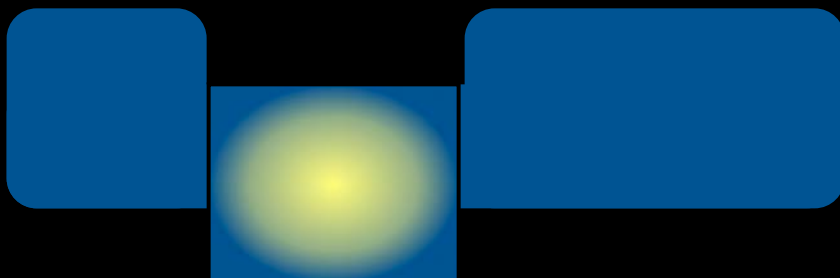
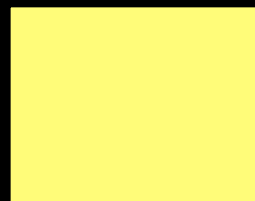
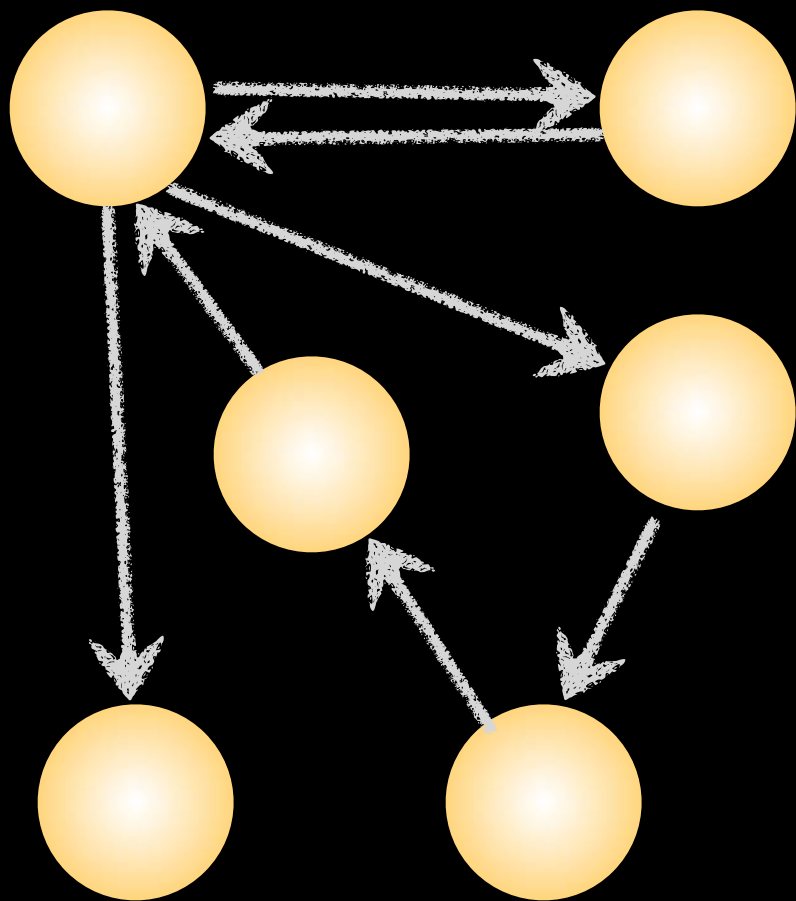
tests → specification-based testing frameworks

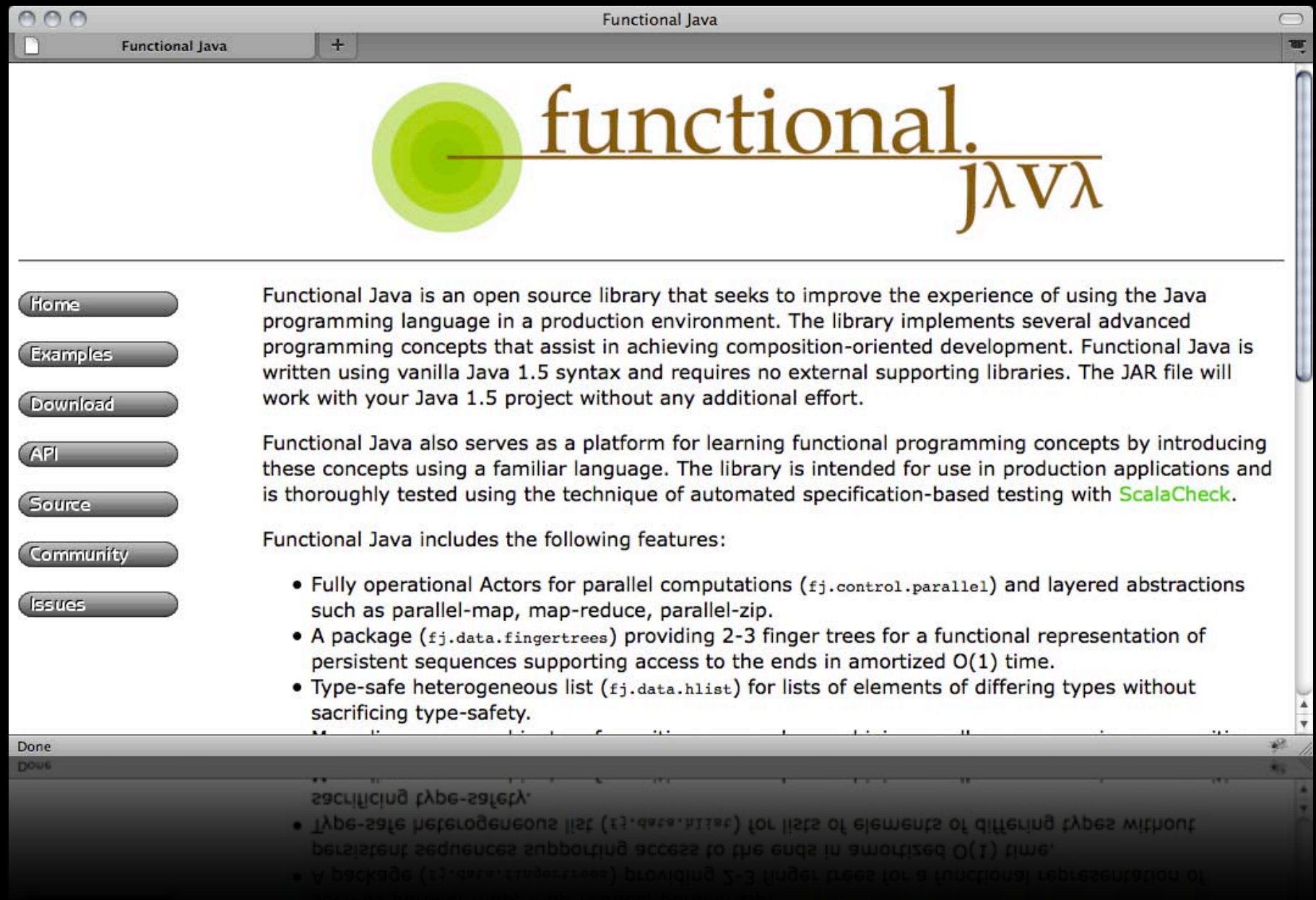


1st-class functions

1st-class functions

functions can
appear anywhere
other language
constructs can
appear





- Home
- Examples
- Download
- API
- Source
- Community
- Issues

Functional Java is an open source library that seeks to improve the experience of using the Java programming language in a production environment. The library implements several advanced programming concepts that assist in achieving composition-oriented development. Functional Java is written using vanilla Java 1.5 syntax and requires no external supporting libraries. The JAR file will work with your Java 1.5 project without any additional effort.

Functional Java also serves as a platform for learning functional programming concepts by introducing these concepts using a familiar language. The library is intended for use in production applications and is thoroughly tested using the technique of automated specification-based testing with [ScalaCheck](#).

Functional Java includes the following features:

- Fully operational Actors for parallel computations (`fj.control.parallel`) and layered abstractions such as parallel-map, map-reduce, parallel-zip.
- A package (`fj.data.fingertrees`) providing 2-3 finger trees for a functional representation of persistent sequences supporting access to the ends in amortized $O(1)$ time.
- Type-safe heterogeneous list (`fj.data.hlist`) for lists of elements of differing types without sacrificing type-safety.

```
public class FNumberClassifier {

    public boolean isFactor(int number, int potential_factor) {
        return number % potential_factor == 0;
    }

    public List<Integer> factorsOf(final int number) {
        return range(1, number+1).filter(new F<Integer, Boolean>() {
            public Boolean f(final Integer i) {
                return number % i == 0;
            }
        });
    }

    public int sum(List<Integer> factors) {
        return factors.foldLeft(add, 0);
    }

    public boolean isPerfect(int number) {
        return sum(factorsOf(number)) - number == number;
    }

    public boolean isAbundant(int number) {
        return sum(factorsOf(number)) - number > number;
    }

    public boolean isDeficiend(int number) {
        return sum(factorsOf(number)) - number < number;
    }
}
```

```
public int sum(List<Integer> factors) {  
    return factors.foldLeft(add, 0);  
}
```

```
public int sum(List<Integer> factors) {  
    return factors.foldLeft(fj.function.Integers.add, 0);  
}
```

```
public int sum(List<Integer> factors) {  
    return factors.foldLeft(fj.function.Integers.add, 0);  
}  
  
public boolean isPerfect(int number) {  
    return sum(factorsOf(number)) - number == 0;  
}  
  
public boolean isAbundant(int number) {  
    return sum(factorsOf(number)) - number > 0;  
}
```

add	F<Integer, F<Integer, Integer>>
multiply	F<Integer, F<Integer, Integer>>
power	F<Integer, F<Integer, Integer>>
remainder	F<Integer, F<Integer, Integer>>
subtract	F<Integer, F<Integer, Integer>>
abs	F<Integer, Integer>

think about results,
not steps

```
public List<Integer> factorsOf(final int number) {  
    return range(1, number+1).filter(new F<Integer, Boolean>() {  
        public Boolean f(final Integer i) {  
            return number % i == 0;  
        }  
    });  
}
```

12

1 2 3 4 5 6 7 8 9 10 11 12

```
public boolean isFactor(int number, int potential_factor) {  
    return number % potential_factor == 0;  
}
```

```
public List<Integer> factorsOf(final int number) {  
    return range(1, number+1).filter(new F<Integer, Boolean>() {  
        public Boolean f(final Integer i) {  
            return number % i == 0;  
        }  
    });  
}
```

```
public int sum(List<Integer> factors) {  
    return factors.foldLeft(0, (f, n) => f + n);  
}
```

think about results,
not steps



List comprehension

```
(defn factors [number]  
  (set (for [n (range 1 (inc number))  
            :when (is-factor? n number)] n)))
```

return the list as a set

for each n in range from 1 to (number + 1)

filter list by criteria my is-factor? function

return the numbers that match

```
(defn is-factor? [factor number]
  (= 0 (rem number factor)))
```

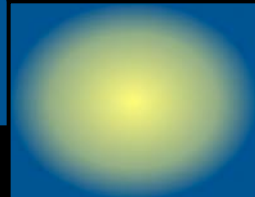
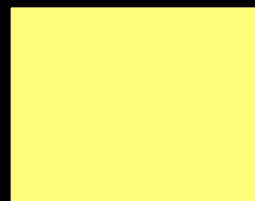
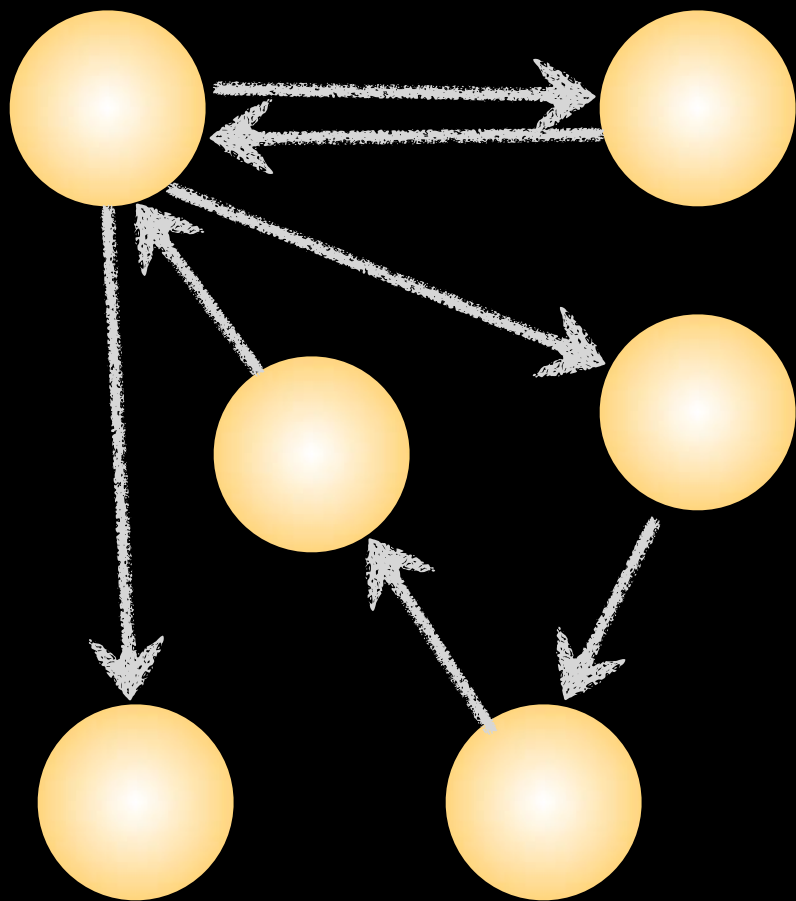
```
(defn factors [number]
  (set (for [n (range 1 (inc number))]
        :when (is-factor? n number) n))))
```

```
(defn sum-factors [number]
  (reduce + (factors number)))
```

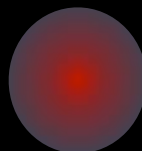
```
(defn perfect? [number]
  (= number (- (sum-factors number) number)))
```



Clojure



composition



academia
alert!



currying

given: $f: (X \times Y) \rightarrow Z$

then: $\text{curry}(f): X \rightarrow (Y \rightarrow Z)$

currying takes a function with a particular number of parameters and returns a function with some of the parameter values fixed, creating a new function

```
def product = { x, y ->  
    return x * y  
}
```

return a version that always multiplies by 4

```
def quadrate = product.curry(4)
```

~~==~~

```
def quadrate_ = { y ->  
    return 4 * y  
}
```



```
def product = { x, y ->  
    return x * y  
}
```

```
def quadrate = product.curry(4)  
def octate = product.curry(8)
```

```
println "4x4: ${quadrate.call(4)}"  
println "5x8: ${octate(5)}"
```

function reuse

```
def adder = { x, y -> x + y }  
def inc = adder.curry(1)
```

```
def composite = { f, g, x -> return f(g(x)) }  
def thirtyTwoer = composite.curry(quadrate, octate)
```

new, different
tools

currying

```
object CurryTest extends Application {  
  
  def filter(xs: List[Int], p: Int => Boolean): List[Int] =  
    if (xs.isEmpty) xs  
    else if (p(xs.head)) xs.head :: filter(xs.tail, p)  
    else filter(xs.tail, p)  
  
  def dividesBy(n: Int)(x: Int) = ((x % n) == 0)  
  
  val nums = List(1, 2, 3, 4, 5, 6, 7, 8)  
  println(filter(nums, dividesBy(2)))  
  println(filter(nums, dividesBy(3)))  
}
```



pure functions

pure
functions

no memory or
i/o side effects

purity

if the result isn't used, it can be removed

a particular invocation with a set of parameters returns a constant value

enables memoization

execution order can change

parallel execution

recursion

iterative filtering

```
def filter(list, criteria) {  
  def new_list = []  
  list.each { i ->  
    if (criteria(i))  
      new_list << i  
  }  
  return new_list  
}
```

```
modBy2 = { n -> n % 2 == 0 }
```

```
l = filter(1..20, modBy2)
```



recursive filtering

```
object CurryTest extends Application {
```

```
  def filter(xs: List[Int], p: Int => Boolean): List[Int] =  
    if (xs.isEmpty) xs  
    else if (p(xs.head)) xs.head :: filter(xs.tail, p)  
    else filter(xs.tail, p)
```

```
  def dividesBy(n: Int)(x: Int) = ((x % n) == 0)
```

```
  val nums = List(1, 2, 3, 4, 5, 6, 7, 8)  
  println(filter(nums, dividesBy(2)))  
  println(filter(nums, dividesBy(3)))
```

```
}
```

think about results,
not steps

<http://www.scala-lang.org/node/135>



think about results,
not steps

what about things you want to control?


performance?

new, different
tools

imperative number classifier

```
public class Classifier6 {  
    private Set<Integer> _factors;  
    private int _number;  
  
    public Classifier6(int number) {...  
  
    private boolean isFactor(int factor) {...  
  
    public Set<Integer> getFactors() {...
```

optimized!



```
        private void calculateFactors() {  
            for (int i = 2; i < sqrt(_number) + 1; i++)  
                if (isFactor(i))  
                    addFactor(i);  
        }  
  
        private void addFactor(int factor) {  
            _factors.add(factor);  
            _factors.add(_number / factor);  
        }  
    }  
}
```

optimized factors

```
public List<Integer> factorsOfOptimized(final int number) {  
    List<Integer> factors = range(1, (int) round(sqrt(number)+1))  
        .filter(new F<Integer, Boolean>() {  
            public Boolean f(final Integer i) {  
                return number % i == 0;  
            }  
        });  
    return factors.append(factors.map(new F<Integer, Integer>() {  
        public Integer f(final Integer i) {  
            return number / i;  
        }  
    }  
    });  
}
```

think about results,
not steps



post-imperative

Google challenged college grads to write code for 100 CPU computers...

...they failed

<http://broadcast.oreilly.com/2008/11/warning-x-x-1-may-be-hazardous.html>

ingrained imperativity

learn MapReduce

<http://code.google.com/edu/submissions/mapreduce-minilecture/listing.html>

sound familiar?

Languages handle

garbage collection

concurrency

state

tests

iteration

...



time

strict
evaluation

academia
alert!



strict
evaluation

all elements
pre-evaluated

divByZero

```
print length([2+1, 3*2, 1/0, 5-4])  
=4
```

non-strict
evaluation

elements evaluated
as needed



Laziness

```
(use '[clojure.contrib.lazy-seqs :only (primes)])
```

```
(def ordinals-and-primes  
  (map vector (iterate inc 1) primes))
```

```
(take 5 (drop 1000 ordinals-and-primes))
```

```
([1001 7927] [1002 7933] [1003 7937] [1004 7949] [1005 7951])
```

new, different
tools



Clojure

concurrency

$$\oint D dA = \int_V \rho dV = Q$$

$$\oint E dl = - \frac{d}{dt} \int_A B dA$$

$$\oint B dA = 0$$

$$\oint H dl = \int_A J dA + \frac{d}{dt} \int_A D dA$$

functions:

depend only on their arguments

given the same arguments, return the same values

no effect on the world

no notion of time

most programs are processes

expect change over time

affect the world

wait for external events

produce different answers at different
times

what can we add
to functional
programming to
deal with
processes?

variables

assume 1 thread of control, 1 timeline

not atomic

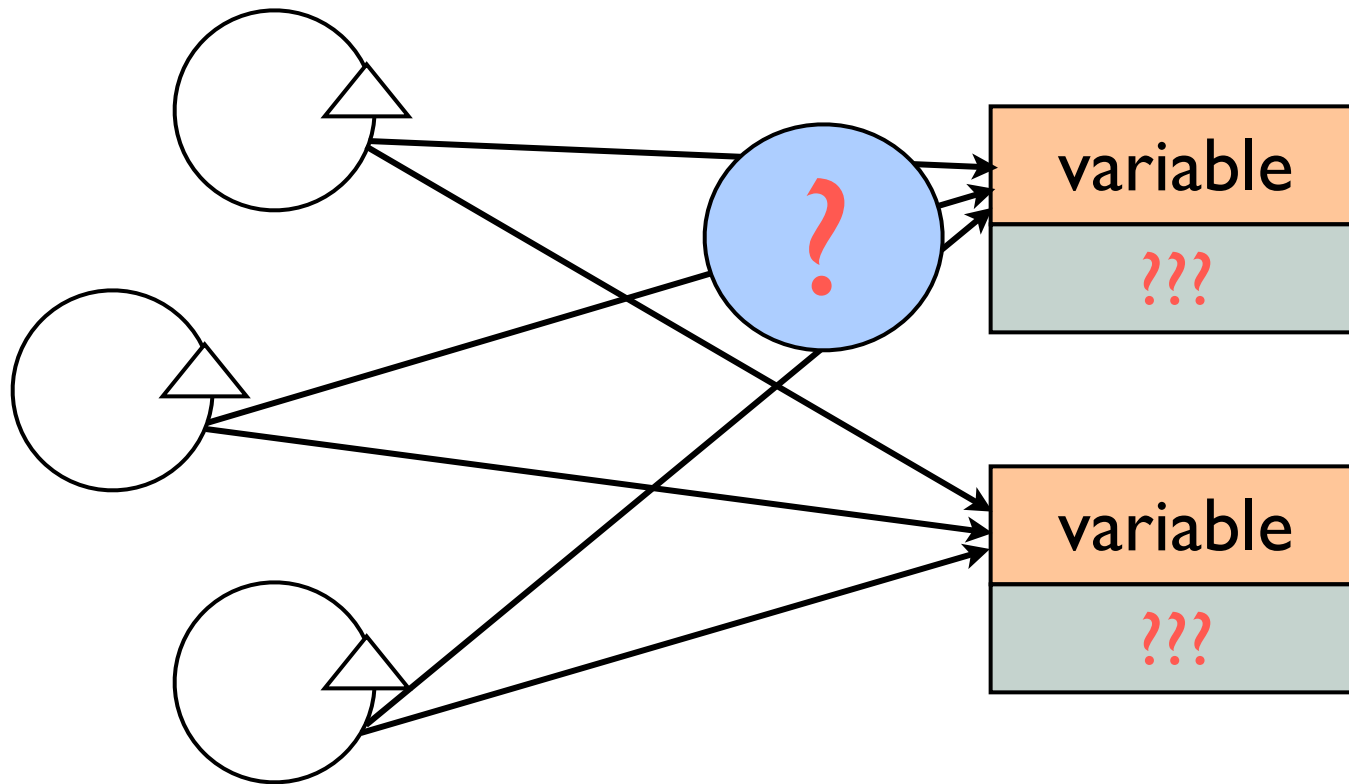
non-composable



subtle visibility rules

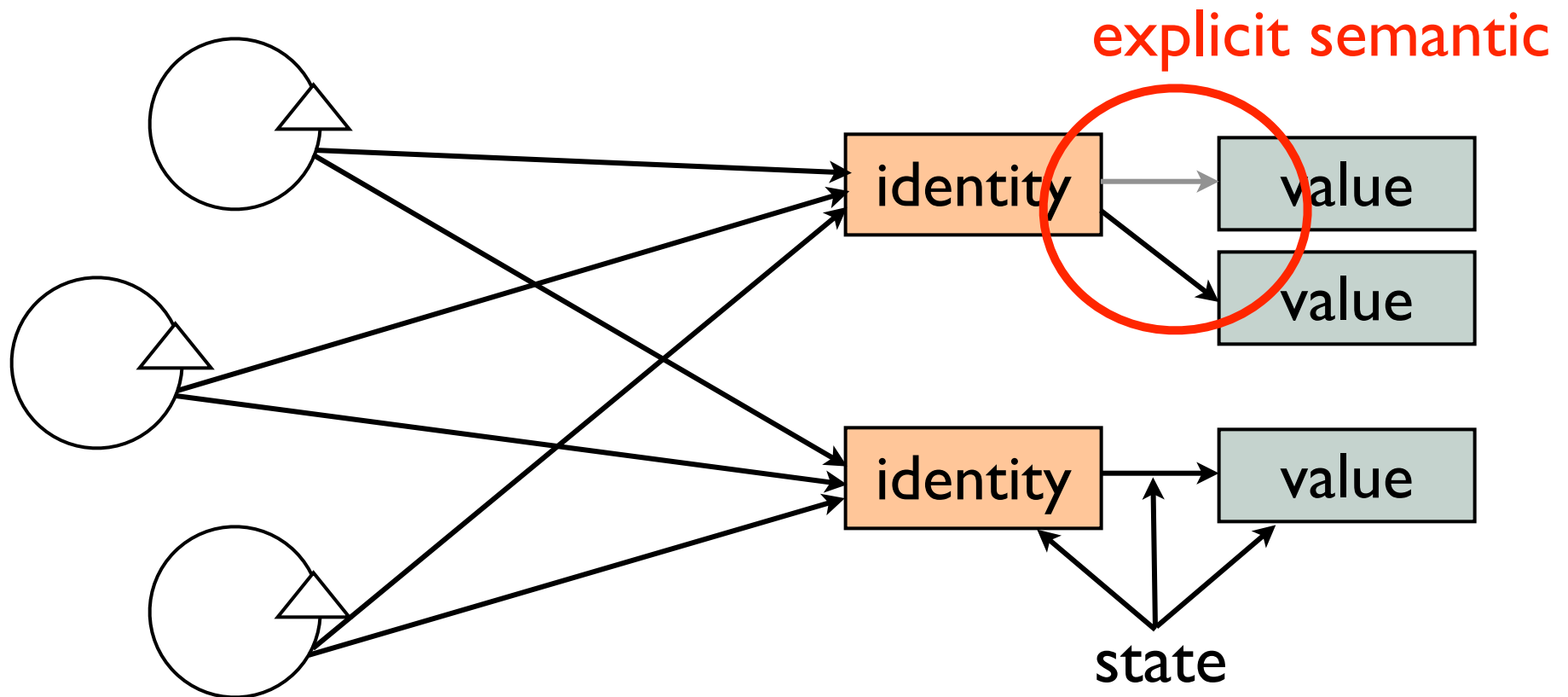
with concurrency: lock & pray

Life w/ variables





identity



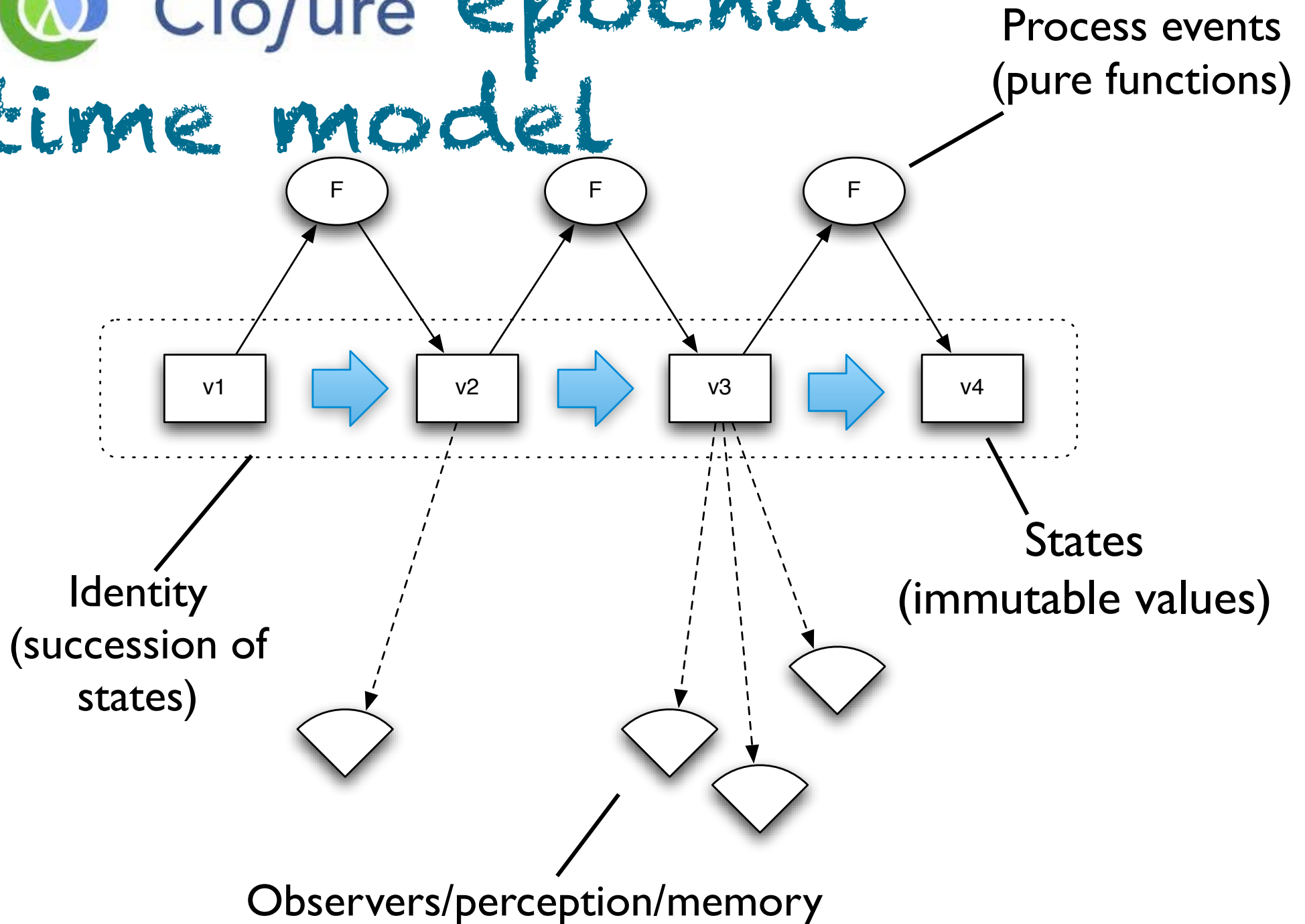
identity, state, & time

term	meaning
value	immutable data in a persistent data structure
identity	series of causally related values over time
state	identity at a point in time
time	relative: before/ simultaneous/after ordering of causal values





Clojure epochal time model



$$\frac{\delta_{ijt} = (v_{ijt} / \sum_{i=1}^n v_{ijt}) \times 100 - (r_{ijt} / \sum_{i=1}^n r_{ijt}) \times 100}{\sigma(\delta_{ij})}$$

actors

```

def isPerfect(candidate: Int) =
{
  val RANGE = 1000000
  val numberOfPartitions = (candidate.toDouble / RANGE).ceil.toInt

  val caller = self

  for (i <- 0 until numberOfPartitions) {
    val lower = i * RANGE + 1;
    val upper = candidate min (i + 1) * RANGE

    actor {
      var partialSum = 0
      for(j <- lower to upper)
        if (candidate % j == 0) partialSum += j

      caller ! partialSum
    }
  }

  var responseExpected = numberOfPartitions
  var sum = 0
  while(responseExpected > 0) {
    receive {
      case partialSum : Int =>
        responseExpected -= 1
        sum += partialSum
    }
  }

  sum == 2 * candidate
}

```

new, different
tools



thinking
functionally



immutability over state transitions

<http://www.ibm.com/developerworks/java/library/j-jtp02183/index.html>

results
over
steps

composition
over
structure

declarative
over
imperative



functional.
JAVA



paradigm
over
load



Clojure



Scala

SUMMARY

$$E = mc^2$$

functional thinking

new ways of thinking about design

new tools for extension, reuse, etc.

immediately beneficial beginning steps

following the general trend in language
design

enables entirely new capabilities



please fill out the session evaluations



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NEAL FORD software architect / meme wrangler

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